

Physics 115 Formulae

$$\begin{aligned}
v &= v_0 + at, \quad \Delta x = \bar{v}t = \frac{1}{2}(v_0 + v)t, \quad \Delta x = v_0 t + \frac{1}{2}at^2, \quad v^2 = v_0^2 + 2a\Delta x, \quad \sum \vec{\mathbf{F}} = m\vec{\mathbf{a}}, \quad F_g = G \frac{m_1 m_2}{r^2}, \quad w = mg, \\
f_s &\leq f_{s,\max} = \mu_s n, \quad f_k = \mu_k n, \quad W = (F \cos \theta) d, \quad KE_t = \frac{1}{2}mv^2, \quad W_{\text{net}} = \Delta KE, \quad W_{nc} = (KE_f + PE_f) - (KE_i + PE_i), \\
PE_g &= mgy, \quad F_s = -kx, \quad PE_s = \frac{1}{2}kx^2, \quad \bar{P} = \frac{W}{\Delta t}, \quad P = Fv, \quad \vec{\mathbf{p}} = m\vec{\mathbf{v}}, \quad \vec{\mathbf{I}} = \vec{\mathbf{F}}_{\text{av}} \Delta t = \Delta \vec{\mathbf{p}} = m\vec{\mathbf{v}}_f - m\vec{\mathbf{v}}_i, \quad \theta = \frac{s}{r}, \\
\omega_{\text{av}} &= \frac{\Delta \theta}{\Delta t}, \quad \alpha_{\text{av}} = \frac{\Delta \omega}{\Delta t}, \quad v_t = r\omega, \quad a_t = r\alpha, \quad a_c = \frac{v^2}{r} = r\omega^2, \quad PE_g = -G \frac{m_1 m_2}{r}, \quad \tau = rF \sin \theta, \quad I_{\text{point mass}} = mr^2, \\
\sum \tau &= I\alpha, \quad KE_r = \frac{1}{2}I\omega^2, \quad L = I\omega, \quad F_e = k_e \frac{|q_1||q_2|}{r^2}, \quad \vec{\mathbf{F}} = q\vec{\mathbf{E}}, \quad E = \frac{k_e|q|}{r^2}, \quad \Delta PE_{\text{el}} = -qE_x \Delta x, \quad \Delta V = \frac{\Delta PE_{\text{el}}}{q}, \\
\Delta V &= -E_x \Delta x, \quad V = k_e \frac{q}{r}, \quad PE_{\text{el}} = k_e \frac{q_1 q_2}{r}, \quad I_{\text{av}} = \frac{\Delta Q}{\Delta t}, \quad I = nqV_dA, \quad R = \frac{\Delta V}{I}, \quad R = \rho \frac{\ell}{A}, \quad \rho = \rho_0[1 + \alpha(T - T_0)], \\
P &= I\Delta V = I^2R = \frac{\Delta V^2}{R}, \quad R_{\text{eq}} = R_1 + R_2 + R_3 + \dots, \quad \frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots, \quad F_{\text{mag}} = qvB \sin \theta, \quad F_{\text{mag}} = BI\ell \sin \theta
\end{aligned}$$

Physics 115 Constants

$$\begin{aligned}
G &= 6.674 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2, \quad R_E = 6.38 \times 10^6 \text{ m}, \quad M_E = 5.98 \times 10^{24} \text{ kg}, \quad g = 9.80 \text{ N/kg}, \quad e = 1.602 \times 10^{-19} \text{ C}, \\
k_e &= 8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2, \quad \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2, \quad \mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}
\end{aligned}$$

Physics 117 Constants

$$\begin{aligned}
\rho_{\text{water}} &= 1.00 \times 10^3 \text{ kg/m}^3, \quad P_{\text{atm}} = 101.3 \text{ kPa}, \quad I_0 = 1.00 \times 10^{-12} \text{ W/m}^2, \quad N_A = 6.022 \times 10^{23} \text{ mol}^{-1}, \\
\sigma &= 5.670 \times 10^{-8} \text{ W/(m}^2\cdot\text{K}^4), \quad k_B = 1.381 \times 10^{-23} \text{ J/K} = 86.1 \text{ }\mu\text{eV/K}, \quad R = 8.314 \text{ J/K}\cdot\text{mol}, \quad 1 \text{ kcal} = 4186 \text{ J}, \\
h &= 6.626 \times 10^{-34} \text{ J}\cdot\text{s} = 4.136 \times 10^{-15} \text{ eV}\cdot\text{s}, \quad \hbar = h/2\pi, \quad c = 2.998 \times 10^8 \text{ m/s}, \quad R_H = 1.097 \times 10^7 \text{ m}^{-1}, \\
a_0 &= 5.29 \times 10^{-11} \text{ m}, \quad r_0 = 1.2 \times 10^{-15} \text{ m}, \quad hc = 1240 \text{ eV}\cdot\text{nm}, \quad k_e e^2 = 1.44 \text{ MeV}\cdot\text{fm}, \quad \text{eV}\cdot\text{nm} = \text{keV}\cdot\text{pm} = \text{MeV}\cdot\text{fm}, \\
m_e &= 9.109 \times 10^{-31} \text{ kg} = 0.00054858 \text{ u} = 0.511 \text{ MeV/c}^2, \quad m_p = 1.673 \times 10^{-27} \text{ kg} = 1.007276 \text{ u} = 938.28 \text{ MeV/c}^2, \\
m_n &= 1.675 \times 10^{-27} \text{ kg} = 1.008665 \text{ u} = 939.57 \text{ MeV/c}^2, \quad m_H = m_p + m_e = 1.007825 \text{ u}, \quad c^2 = 931.494 \text{ MeV/u}
\end{aligned}$$

Standard Prefixes Used to Denote Multiples of Ten

Prefix	Symbol	Factor
Tera	T	10^{12}
Giga	G	10^9
Mega	M	10^6
Kilo	k	10^3
Hecto	h	10^2
Deka	da	10^1
Deci	d	10^{-1}
Centi	c	10^{-2}
Milli	m	10^{-3}
Micro	μ	10^{-6}
Nano	n	10^{-9}
Pico	p	10^{-12}
Femto	f	10^{-15}

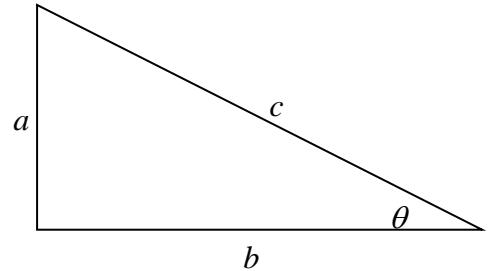
Basic Mathematical Formulae

$$\begin{aligned}
\text{Area of a circle} &= \pi r^2 \\
\text{Circumference of a circle} &= 2\pi r \\
\text{Surface area of a sphere} &= 4\pi r^2 \\
\text{Volume of a sphere} &= \frac{4}{3}\pi r^3 \\
\text{Volume of a cylinder} &= \pi r^2 h \\
\text{Pythagorean theorem:} \\
&c^2 = a^2 + b^2 \\
\text{Trigonometric relations:} \\
\sin \theta &= \text{opp/hyp} = a/c \\
\cos \theta &= \text{adj/hyp} = b/c \\
\tan \theta &= \text{opp/adj} = \frac{a}{b} = \frac{\sin \theta}{\cos \theta}
\end{aligned}$$

Quadratic formula:

If $ax^2 + bx + c = 0$, then

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



Physics 117 Formulae

$$\rho = \frac{M}{V}, \quad P_{\text{av}} = \frac{F}{A}, \quad \frac{F}{A} = Y \frac{\Delta L}{L_0}, \quad \frac{F}{A} = S \frac{\Delta x}{h}, \quad \Delta P = -B \frac{\Delta V}{V}, \quad P_2 = P_1 + \rho g(y_1 - y_2), \quad P_{\text{gauge}} = P_{\text{absolute}} - P_0,$$

$$B = \rho_{\text{fluid}} V_{\text{fluid}} g, \quad \rho_1 A_1 v_1 = \rho_2 A_2 v_2, \quad A_1 v_1 = A_2 v_2, \quad P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2, \quad \frac{\Delta V}{\Delta t} = \frac{\pi R^4 (P_1 - P_2)}{8 \eta L},$$

$$F_r = 6\pi\eta rv, \quad F_s = -kx, \quad PE_s = \frac{1}{2}kx^2, \quad \omega = 2\pi f = \frac{2\pi}{T} = \sqrt{\frac{k}{m}}, \quad T = 2\pi \sqrt{\frac{L}{g}}, \quad T = 2\pi \sqrt{\frac{I}{mgL}}, \quad x = A \cos(2\pi ft),$$

$$v_x = -A\omega \sin(2\pi ft), \quad a_x = -A\omega^2 \cos(2\pi ft), \quad v = \frac{\lambda}{T} = f\lambda, \quad v = \sqrt{\frac{F}{\mu}}, \quad v = (331 \text{ m/s}) \sqrt{\frac{T}{273 \text{ K}}}, \quad I = \frac{P}{A}, \quad \beta = 10 \log\left(\frac{I}{I_0}\right),$$

$$f_o = \left(\frac{v + v_o}{v - v_s} \right) f_s, \quad r_2 - r_1 = n\lambda, \quad r_2 - r_1 = (n + \frac{1}{2})\lambda, \quad d_{\text{NN}} = \frac{1}{2}\lambda, \quad f_b = |f_2 - f_1|, \quad \frac{\sin \theta_2}{\sin \theta_1} = \frac{v_2}{v_1}, \quad n_1 \sin \theta_1 = n_2 \sin \theta_2,$$

$$n = \frac{c}{v}, \quad M = \frac{h'}{h} = -\frac{q}{p}, \quad \frac{1}{p} + \frac{1}{q} = \frac{1}{f}, \quad \frac{1}{f} = (n-1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right), \quad \delta = r_2 - r_1 = d \sin \theta, \quad d \sin \theta_{\text{bright}} = m\lambda,$$

$$d \sin \theta_{\text{dark}} = (m + \frac{1}{2})\lambda, \quad \sin \theta_{\text{dark}} = m \frac{\lambda}{a}, \quad P = \frac{1}{f}, \quad m = \frac{\theta}{\theta_0}, \quad m = \frac{N}{p} = \frac{25 \text{ cm}}{p}, \quad m = M_1 m_e = -\frac{L}{f_o} \left(\frac{25 \text{ cm}}{f_e} \right),$$

$$\sin \theta \geq \frac{1.22\lambda}{a}, \quad T_C = T - 273.15, \quad \Delta L = \alpha L_0 \Delta T, \quad \Delta A = 2\alpha A_0 \Delta T, \quad \Delta V = \beta V_0 \Delta T, \quad PV = Nk_B T = nRT,$$

$$\frac{1}{2}mv_{\text{rms}}^2 = \frac{3}{2}k_B T, \quad Q = mc\Delta T, \quad P_{\text{net}} = \sigma Ae(T^4 - T_0^4), \quad P = kA \frac{(T_h - T_c)}{L}, \quad \lambda_{\text{max}} T = 2.898 \times 10^{-3} \text{ m} \cdot \text{K}, \quad E = hf = \frac{hc}{\lambda},$$

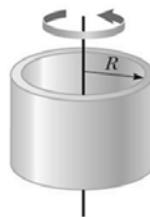
$$KE_{\text{max}} = e\Delta V_s = hf - \phi, \quad \lambda - \lambda_0 = \frac{h}{m_e c}(1 - \cos \theta), \quad p = \frac{E}{c} = \frac{h}{\lambda}, \quad \lambda = \frac{h}{p} = \frac{h}{mv}, \quad \frac{1}{\lambda} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right), \quad r_n = \frac{n^2}{Z} a_o$$

$$E_n = -\frac{13.6(Z^2)}{n^2} \text{ eV}, \quad \Delta E = (\Delta m)c^2, \quad r = r_0 A^{1/3}, \quad R = \lambda N, \quad N = N_0 e^{-\lambda t} = N_0 \left(\frac{1}{2} \right)^m \quad T_{1/2} = \frac{\ln 2}{\lambda} = \frac{0.693}{\lambda}$$

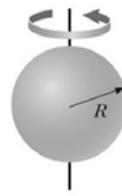
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Table 8.1 Moments of Inertia for Various Rigid Objects of Uniform Composition

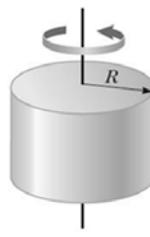
Hoop or thin cylindrical shell
 $I = MR^2$



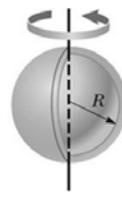
Solid sphere
 $I = \frac{2}{5}MR^2$



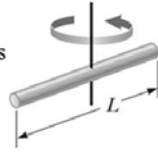
Solid cylinder or disk
 $I = \frac{1}{2}MR^2$



Thin spherical shell
 $I = \frac{2}{3}MR^2$



Long, thin rod with rotation axis through centre
 $I = \frac{1}{12}ML^2$



Long, thin rod with rotation axis through end
 $I = \frac{1}{3}ML^2$

